

8 Section 14.1

- Vector function:

$$\vec{r}(t) = \langle f(t), g(t), h(t) \rangle$$

where f, g, h are component functions.

- Parametric equations of a space curve C :

$$\vec{r} = \vec{r}(t) = \langle x, y, z \rangle \Leftrightarrow \begin{cases} x = f(t) \\ y = g(t) \\ z = h(t) \end{cases}$$

- Limit of a vector function:

$$\lim_{t \rightarrow a} \vec{r}(t) = \langle \lim_{t \rightarrow a} f(t), \lim_{t \rightarrow a} g(t), \lim_{t \rightarrow a} h(t) \rangle$$

9 Section 14.2

- Derivative:

$$\vec{r}'(t) = \langle f'(t), g'(t), h'(t) \rangle = \lim_{h \rightarrow 0} \frac{\vec{r}(t+h) - \vec{r}(t)}{h}$$

- $\vec{r}'(t)$ is the direction vector of the tangent line to the curve $\vec{r} = \vec{r}(t)$ at the point $P(f(t), g(t), h(t))$. Unit tangent vector

$$\vec{T}(t) = \frac{\vec{r}'(t)}{|\vec{r}'(t)|}$$

- Integral $\int \vec{r}'(t) dt = \langle \int f'(t) dt, \int g'(t) dt, \int h'(t) dt \rangle$

10 Section 14.3

- Length of a curve between $P(f(a), g(a), h(a))$ and $Q(f(b), g(b), h(b))$:

$$L = \int_a^b |\vec{r}'(t)| dt = \int_a^b \sqrt{f'(t)^2 + g'(t)^2 + h'(t)^2} dt$$

- Arc length function

$$S(t) = \int_a^t |\vec{r}'(u)| du, \quad \frac{ds}{dt} = |\vec{r}'(t)|$$

- Curvature:

$$\kappa = \left| \frac{d\vec{T}}{ds} \right| = \frac{|\vec{T}'(t)|}{|\vec{r}'(t)|}$$

- Unit normal vector:

$$\vec{N}(t) = \frac{\vec{T}'(t)}{|\vec{T}'(t)|}$$

- Unit binormal vector:

$$\vec{B}(t) = \vec{T}(t) \times \vec{N}(t)$$