

4 Section 13.4

- Cross product: $\vec{a} = \langle a_1, a_2, a_3 \rangle$, $\vec{b} = \langle b_1, b_2, b_3 \rangle$,

$$\vec{a} \times \vec{b} = \langle a_2b_3 - a_3b_2, a_3b_1 - b_3a_1, a_1b_2 - a_2b_1 \rangle$$

- Determinant formula:

$$\vec{a} \times \vec{b} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$

- Properties:

$$\vec{a} \times \vec{a} = \vec{0}, \quad \vec{a} \times \vec{b} = -\vec{b} \times \vec{a}, \quad \vec{a} \perp \vec{b} \Leftrightarrow \vec{a} \times \vec{b} = 0$$

- Area of parallelogram:

$$|\vec{a} \times \vec{b}| = |\vec{a}| |\vec{b}| \sin \theta$$

- Scalar triple product: $\vec{a} = \langle a_1, a_2, a_3 \rangle$, $\vec{b} = \langle b_1, b_2, b_3 \rangle$, $\vec{c} = \langle c_1, c_2, c_3 \rangle$,

$$\vec{a} \cdot (\vec{b} \times \vec{c}) = \begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix}$$

$$\text{Volume of parallelepiped} = |\vec{a} \cdot (\vec{b} \times \vec{c})|$$

$$\vec{a}, \vec{b}, \vec{c} \text{ coplanar} \Leftrightarrow \vec{a} \cdot (\vec{b} \times \vec{c}) = 0.$$

5 Section 13.5

Equations of lines: $\vec{r} = \langle x, y, z \rangle$, $\vec{r}_0 = \langle x_0, y_0, z_0 \rangle$, $P(x_0, y_0, z_0)$ point on the line.

- Vector equation:

$$\vec{r} = \vec{r}_0 + t\vec{v} \Leftrightarrow \langle x, y, z \rangle = \langle x_0, y_0, z_0 \rangle + t \langle a, b, c \rangle$$

- Parametric equations:

$$\begin{cases} x = x_0 + at \\ y = y_0 + bt \\ z = z_0 + ct \end{cases}$$

- Symmetric equation: $\vec{v} = \langle a, b, c \rangle$ a direction vector of the line

$$\frac{x - x_0}{a} = \frac{y - y_0}{b} = \frac{z - z_0}{c}$$