

MATH 251  
Exam I  
July 16, 2009

ANSWER KEY

1. (a) E (b) H (c) D (d) A

2.  $y = \sqrt{2e^t - 1}$

3. (a)  $Q' + \frac{Q}{50} = 8, \quad Q(0) = 100$

(b)  $Q(t) = 400 - 300e^{-t/50}$

(c)  $\lim_{t \rightarrow \infty} Q(t) = 400$

4. (a)  $(0, \infty)$  (b)  $y = \frac{1}{64}t^3 - \frac{1}{2}t$

5. (a)  $y = 3e^t - e^{4t}$  (b)  $\lim_{t \rightarrow \infty} y(t) = -\infty$

6.  $W(y_1, y_2)(t) = t^4 \neq 0$

7.  $y = C_1 t + C_2 t^{-2}$

8.  $y = C_1 e^t + C_2 e^{-t} + A \cos(2t) + B \sin(2t) + (Ct^2 + Dt)e^t + E \cos(t) + F \sin(t)$

9. (a) *iii* (b)  $y = e^t + te^t$