

Math 22 Section 9

Quiz 9 Solutions

1. Evaluate the following expressions:

(a) $\log_6(6^4)$

$$\log_6(6^4) = 4\log_6(6) = 4$$

(b) $\log_3(\frac{1}{9})$

$$\log_3(\frac{1}{9}) = -2\log_3(3) = -2$$

(c) $e^{\ln 5}$

$$e^{\ln 5} = 5$$

(d) $2\log_{12}3 + 2\log_{12}4$

$$2\log_{12}3 + 2\log_{12}4 = \log_{12}(3^2 4^2) = \log_{12}(12^2) = 2$$

2. Find the domain and vertical asymptote of

$$f(x) = \log_3(x - 1) - 2$$

domain $(1, \infty)$

vertical asymptote $x = 1$

3. Expand the expression:

(a) $\log_5\left(\frac{x}{2}\right)$

$$\log_5\left(\frac{x}{2}\right) = \log_5(x) - \log_5(2)$$

(b) $\ln(x^3e^{2x})$

$$\ln(x^3e^{2x}) = \ln(x^3) + \ln(e^{2x}) = 3\ln(x) + 2x$$

4. Combine the expression:

(a) $\log(12) - \frac{1}{2}\log(9) - \log(2)$

$$\log(12) - \frac{1}{2}\log(9) - \log(2) = \log\left(\frac{12}{(3)(2)}\right) = \log(2)$$

(b) $\ln(5) + 2\ln(x) + 3\ln(x^2 + 5)$

$$\ln(5) + 2\ln(x) + 3\ln(x^2 + 5) = \ln(5x^2(x^2 + 5)^3)$$