

$$\textcircled{1} \quad t^2 - 8t + 15 \geq 0$$

$$(t-5)(t-3) \geq 0$$

$$t \leq 3 \text{ or } t \geq 5$$

Using interval notation, $(-\infty, 3] \cup [5, \infty)$.

$$\textcircled{2} \quad T(x+h) - T(x-h) = 3(x+h)^2 - 2(x+h) - \{3(x-h)^2 - 2(x-h)\}$$

$$= 3(x^2 + 2hx + h^2) - 2x - 2h - \{3(x^2 - 2hx + h^2) - 2x + 2h\}$$

$$= 3x^2 + 6hx + 3h^2 - 2x - 2h - 3x^2 + 6hx - 3h^2 + 2x - 2h$$

$$= 12hx - 4h$$

$\textcircled{3}$ Domain of f is the set of all real numbers, say $(-\infty, \infty)$.

$$f(x) = x^2 - 2x = (x-1)^2 - 1 \text{ gives the range of } f = [-1, \infty).$$

$\textcircled{4}$ Since $y = x^2 - 8x + 2$ opens upward, it has the minimum value.

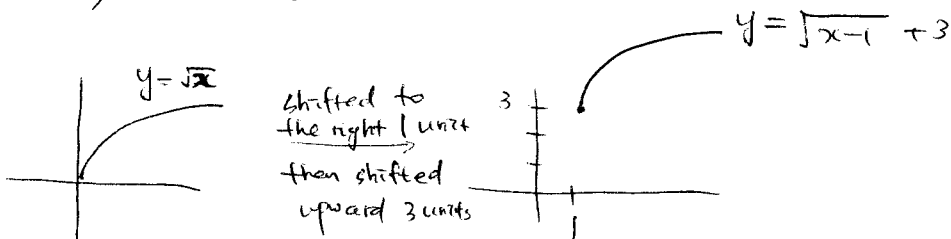
$$y = (x-4)^2 - 14 \Rightarrow \text{vertex } (4, -14) \text{ The minimum value is } -14.$$

$$\textcircled{5} \quad f^{-1}(10) = -3 \Leftrightarrow f(-3) = 10$$

$$\Rightarrow \frac{2-2t}{2+2t} = -3 \Rightarrow 2-2t = -3(2+2t) \Rightarrow 2-2t = -6-6t$$

$$\Rightarrow 4t = -8 \Rightarrow t = -2.$$

$\textcircled{6}$



$\textcircled{7}$ Looking at the inside of $f(x)$. Set $g(x) = x^2 - 4x + 20 \Rightarrow g(x) = (x-2)^2 + 16$.

$\Rightarrow g$ has the minimum value 16 at $x=2$.

$\Rightarrow f$ has the minimum value $\sqrt{16} = 4$ at $x=2$.

$$\textcircled{8} \quad (g \circ f)(x) = g(f(x)) = g(5x+1) = -2(5x+1) - 5 = -10x - 2 - 5 = -10x - 7.$$

$\textcircled{9}$

